

# ARCTIC: Approximate Real-Time Computing in a Cache-Conscious Multicore Environment

Sangeet Saha<sup>§</sup>, Shounak Chakraborty<sup>§</sup>, Sukarn Agarwal, Magnus Sjölander, and Klaus D. McDonald-Maier

**Abstract**—Improving result-accuracy in approximate computing (AC) based time-critical systems, without violating power constraints of the underlying circuitry, is gradually becoming challenging with the rapid progress in technology scaling. The execution span of each AC real-time tasks can be split into a couple of parts: (i) the mandatory part, execution of which offers a result of acceptable quality, followed by (ii) the optional part, which can be executed partially or completely to refine the initially obtained result in order to increase the result-accuracy, while respecting the time-constraint. In this article, we introduce a novel hybrid offline-online *scheduling strategy*, ARCTIC, for AC real-time tasks. The goal of real-time scheduler of ARCTIC is to maximise the results-accuracy (QoS) of the task-set with opportunistic shedding of the optional part, while respecting system-wide constraints. During execution, ARCTIC retains exclusive copy of the private cache blocks only in the local caches in a multi-core system and no copies of these blocks are maintained at the other caches, and improves performance (i.e., reduces execution-time) by accumulating more live blocks on-chip. Combining offline scheduling with the online cache optimization improves both QoS and energy efficiency. While surpassing prior arts, our proposed strategy reduces the task-rejection-rate by up to 25%, whereas enhances QoS by 10%, with an average energy-delay-product gain of up to 9.1%, on an 8-core system.

**Index Terms**—Real-time systems, Approximate Computing, QoS Improvement, Energy Efficiency, Cache Management

## I. INTRODUCTION

In time-constrained systems, functional correctness not only depends on the result-accuracy, but also that results are produced before given deadlines [35]. For such real-time scenarios, approximated result obtained before the deadline is preferable over an accurate result produced after the deadline. In a plethora of application areas, such as multimedia processing, tracking of mobile targets, real-time heuristic search, information gathering and control systems, an approximate result, obtained within the time-limit is usually acceptable [7]. For example, in the case of video streaming applications, frames with lower quality are preferable over completely missing frames. In the case of target tracking, an approximated estimation of the target's location produced within the deadline is preferred to an accurate location, obtained too late. In such domains, applications are usually modeled as real-time

task graphs, or precedence constrained task graphs (PTGs), whose nodes denote application tasks and edges denote inter-task dependencies. Further, each of these tasks is logically decomposed into a mandatory part and an optional part [12], [34], [36].

The entire mandatory part has to be completed prior to the deadline to generate minimally acceptable QoS, followed by a partial/complete execution of the optional part, subject to availability of system resources, to improve accuracy of the initially obtained result within the deadline. The QoS increases with the number of execution cycles spent on the optional part, and based upon the amount of execution cycles of the optional part, a task can offer various QoS levels. However, it is worth noting that, compared to a lower QoS level, a higher QoS level demands additional computation, which consequently leads to higher execution time and associated energy overheads. Thus, the desire for enhanced QoS with improved energy efficiency and the completing tasks within their deadlines are often in conflict with each other. Hence, *given a real-time application modeled as a PTG, where the tasks have multiple QoS levels and need to be scheduled on a multiprocessor platform, maximising system-level QoS by allocating appropriate quality levels, cores, and execution start times to the tasks, and assigning core frequency, while satisfying all timing, power, precedence, and resource-related constraints, is a challenging scheduling problem.*

Approximate real-time scheduling techniques are often classified as offline or online, based on whether scheduling decisions are made at design time or at runtime [18]. Prior art considered approximate computing based offline real-time task scheduling [12], [36] by focusing on the processor cores from a power-performance perspectives in case of chip multiprocessor (CMP) based systems. As time-constrained systems require a high degree of timing predictability, it is typically preferable to employ offline scheduling algorithms for such systems, as this allows all timing requirements to be specified offline before execution [43]. However, rigid adherence to static schedules during online execution could result in reduced performance, if the runtime architectural characteristics are not considered [13].

Architectural techniques are effective in improving the energy efficiency of the last level caches (LLCs) [14]–[16], [39]. A prior coherence management technique for shared LLC, proposed by Lodde et al., shrinks LLC size dynamically at the way level granularity, while maintaining only copies of the private blocks in the local cache [31]. Later Albericio et al. proposed a “reuse cache” that decouples tag and data for unused LLC blocks [5] and improves performance, while

S.Saha and K. McDonald-Maier are with the Embedded and Intelligent Systems Lab, University of Essex, Colchester, UK. S. Chakraborty and M. Sjölander is with the Department of Computer Science, Norwegian University of Science and Technology, Trondheim, Norway. S. Agarwal is with the School of Computing and Electrical Engineering, IIT Mandi, India.

e-mail: (sangeet.saha@essex.ac.uk, shounak.chakraborty@ntnu.no, sukarn@iitmandi.ac.in, magnus.sjlander@ntnu.no, kdm@essex.ac.uk).

<sup>§</sup>Equal contribution

incurring 16% additional LLC storage, associated with a noticeable power overhead. ARCTIC introduces a critical management of the private blocks in a shared LLC to improve both power efficiency and performance, by increasing live-block count in the LLC, without incurring noticeable overheads. We argue and empirically validate that our novel runtime architectural technique to improve performance as well as energy efficiency can also generate a slack time before the deadline by reducing the task's execution span. Such slacks can also be exploited either to maximise QoS by executing more from the optional part of the task or to enhance energy efficiency of the underlying hardware by enabling power gating mode [38]. However, *it is worth noting that, even in these situations, static schedules are still crucial as they can serve as the basis for further online QoS stimulation considering runtime characteristics of the task.*

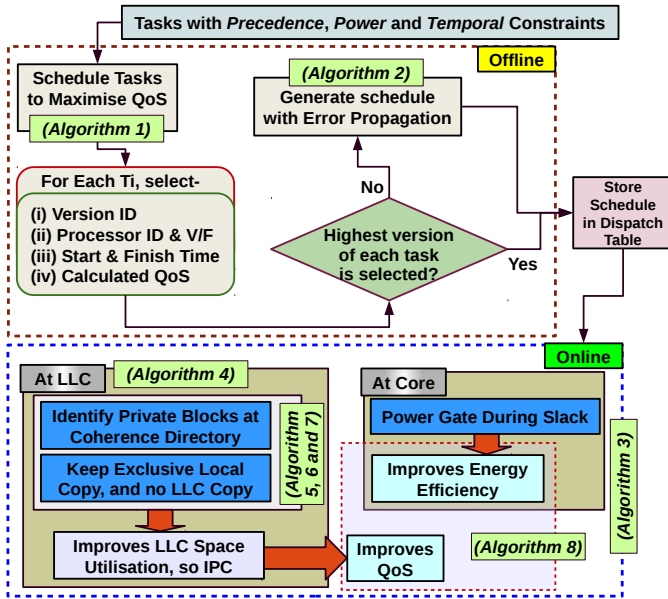


Fig. 1: ARCTIC: Process Overview

In this paper, we propose a scheduling technique, ARCTIC, for approximate real-time task-set that generates a schedule in offline with an objective to maximise the QoS, which is further enhanced along with significant energy reduction at runtime. Our considered task-set is dependent and hence can be represented by a PTG (Sec. III), are scheduled on a CMP, where each task can have multiple versions with distinct degrees of accuracy. The entire concept of ARCTIC is shown in Figure 1, where the upper half of the figure depicts the offline part and the lower part elaborates the online part. Respective algorithms in Figure 1 for individual sub-stages of ARCTIC-Offline and ARCTIC-Online which will be elaborated in Sec. IV and V, respectively.

Our key contributions can be summarized as follows:

- ARCTIC-Offline is a **power constrained based task-scheduling** strategy (Sec. IV) that is formulated initially as an optimization problem to maximise QoS, which is solved to generate an optimal schedule. Each task is assigned to a processor core along with a voltage and frequency setting.

- In cases where tasks are scheduled with lower accuracy, the portions of the optional parts that have not been scheduled are added with the successor task(s) to enhance QoS. This phenomenon is termed as **Error Propagation**, which might cause a deadline violation, that is however ameliorated by **readjusting the voltage and frequency** at task level granularity, without violating the power-budget (Sec. IV).
- At runtime, ARCTIC-Online maintains **exclusive copies of the private LLC blocks** in the respective local caches, and thus frees up space in the shared LLC (Sec. V), that are exploited to accumulate more live LLC blocks to improve performance.
- The **slacks generated by reduced execution-times are exploited** either to enhance QoS by executing more from optional parts of the tasks, or to improve energy efficiency by turning off the cores (Sec. V).

While surpassing prior arts, ARCTIC-Offline reduces the task-rejection-rate by up to 25%, whereas ARCTIC-Online enhances QoS further, by 10%, with an average energy-delay-product (EDP) gain of up to 9.1%, for an 8-core based CMP (Sec. VI).

## II. RELEVANT PRIOR ART

In recent years, researchers have developed various approaches for the real-time scheduling of PTGs on multicore platforms. One set of the approaches are focused on energy-minimisation. Since many of the CMP-based real-time systems are battery-powered, reducing energy in such systems has become an active research topic in recent past [6], [37]. For energy savings, DVFS (dynamic voltage frequency scaling) and DPM (dynamic power management) are typically employed. Scheduling time-constrained dependent tasks on the CMP platform by considering the energy/power cap is however becoming challenging with technology scaling [9]. An ILP-based optimal approach was employed to solve the problem in a prior art [17]. However, incorporating DVFS with task allocation and scheduling decision is not straightforward, as additional variables regarding the core selection, data dependency, and Voltage/frequency (V/F) selection are required. Moreover, these variables are interconnected, which makes the problem challenging. To tackle this problem, researchers applied system-level DVFS, where the frequency of each processor was not adjusted individually. But, this technique is not suitable for time-constrained systems. Researchers attempted to build up sub-optimal energy-aware scheduling strategies for real-time task sets with different system-wide constraints [24], [33], [46].

In 2013, Kim considered QoS-based real-time scheduling problem to improve the overall QoS under task deadlines [25]. Subsequently, research into QoS-aware real-time scheduling has emerged. The concept of approximate computing to meet the energy budget of a large-scale real-time system was introduced for independent tasks [12]. Zhou et al. [48] took energy consumption into account and proposed an energy-adaptive and QoS-driven task mapping method. The energy-efficient scheduling of the dependent approximate tasks was

considered in some prior arts [30], [36] with DVFS at the cores. However, these methods did not consider the effect on system performance when QoS degradation occurs for a task, and the proposed optimal approaches also suffer from high computational complexity. In some recent works [13], [39], thermal efficient task scheduling for dependent approximate real-time tasks was discussed, where the QoS offered in offline mode is further enhanced by employing runtime architectural techniques. In ARCTIC, a low-complexity optimal offline task scheduling technique is proposed to maximise QoS. This obtained QoS is further enhanced by incorporating runtime architectural parameters. Moreover, to realistically frame the behavior of QoS-aware systems, we introduce the concept of error propagation.

Improving QoS as well as energy efficiency by employing runtime architectural techniques can be a viable option to be considered in approximate real-time computing. To reduce leakage power and area occupancy of the conventional MOSFET-based LLC, Lodde et al. proposed a decoupled technique for data and tag entries of the LLC [31]. The private blocks are placed only in the local cache, and LLC data array is trimmed to be used only for the shared blocks. This technique significantly saves leakage power, but at the cost of performance loss up to 10%. Later, Albericio et al. proposed a tag/data decoupled technique that keeps both data and tag only for the blocks that have been reused [5]. This policy leads to a 16% increase in (MOSFET-based) LLC storage capacity; however, authors did not consider the power consumption of the LLC. In a recent study, researchers exploit dataless LLC entries to overcome several write issues in an NVM-based hybrid LLC [3], [4]. Another recent approach attempted to reduce refresh counts in an embedded-DRAM-based LLC by segregating the private blocks and decoupled tag and data for such blocks [32]. A coherence protocol based private block management was also proposed [40], which incurs overhead to the coherence management. Most of these prior policies limit usages of the data array either to reduce leakage consumption of the MOSFET-based LLC or to overcome writing issues of the NVM caches. In ARCTIC, we considered FinFET-based LLC that consumes lower leakage than the MOSFET-based LLC and do not have writing issues like NVMs. Hence, in ARCTIC, by managing the private blocks, the freed-up LLC space is exploited to enhance the overall performance.

### III. SYSTEM MODEL AND ASSUMPTIONS

Our considered CMP consists of  $m$  homogeneous cores, denoted as  $P = P_1, P_2, \dots, P_m$ . Each core can support  $L$  distinct V/F settings, denoted as  $V = V_1, V_2, \dots, V_L$  and  $F = F_1, F_2, \dots, F_L$ , where  $V_i < V_{i+1}$  and  $F_i < F_{i+1}$ . Our considered application, which is collection of a set of sub-applications (also termed tasks in this paper), can be represented as a PTG (see Figure 2),  $G = (T, E)$ , where  $T$  is a set of nodes ( $T = T_i | 1 \leq i \leq n$ ) and  $E$  is a set of directed edges ( $E = \{(T_i, T_j) | 1 \leq i, j \leq n; i \neq j\}$ ). Each node  $T_i$  denotes a task of the PTG, and each directed edge specifies an execution order that the  $T_j$  can only start after the task  $T_i$  is completed. Being a real-time application,  $G$  has to be executed

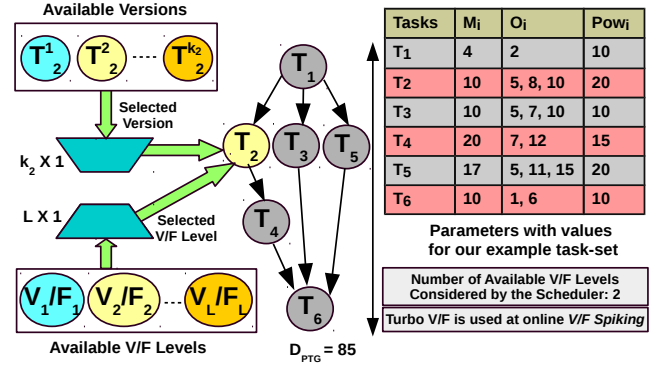


Fig. 2: Precedence task graph (PTG) with timing parameters and power requirements.

within the given deadline, by executing all the associated task ( $T_i$ ). The end-to-end application deadline is assumed to be  $D_{PTG}$ . We also assume that,  $T_i$  can have  $k_i$  different versions,  $T_i = T_i^1, T_i^2, \dots, T_i^{k_i}$ , those are distinct by their respective execution lengths ( $O_i$ ), denoted as  $O_i^1, O_i^2, \dots, O_i^{k_i}$ , where  $O_i^p$  offers higher result-accuracy than  $O_i^q$ , if  $p > q$ . For each optional part of a task ( $O_i$ ), there exists a separate executable module, that is executed after execution of the mandatory portion ( $M_i$ ) of the respective task,  $T_i$ . The length of the  $j$ -th version of task  $T_i$  ( $len_i^j$ ) can be defined as:  $len_i^j = M_i + O_i^j$ . Note that,  $len_i^j$  includes the cycles required for accessing LLC, which we obtain by executing an individual task for a particular configuration. We define result-accuracy  $Acc_i^j$  of  $T_i^j$  as the executed optional part of the task,  $O_i^j$  (i.e.,  $Acc_i = O_i^j$ ). Thus, the overall system level result-accuracy (QoS) is now defined as the sum of the executed cycles of  $O_i^j$  for all the tasks [12], which can be represented as:  $QoS = \sum_{i=1}^n O_i^j | T_i = T_i^j$ .

### IV. ARCTIC-Offline

With an objective to maximise the QoS, subject to the system-wide constraints, ARCTIC-Offline allocates tasks to the processor cores with the assigned V/F. Our scheduling problem is bounded by a set of constraints and the problem is detailed in Sec. IV-A. We further discuss the concept of error propagation in Sec. IV-B, before concluding the section with a working example.

#### A. ARCTIC: ILP based Scheduling

We present a scheduling strategy based on integer linear programming (ILP). For this purpose, we first introduce an integer decision variable  $S_i \in \mathbb{Z}^+$  to capture the start time of each task  $T_i$ , where  $\mathbb{Z}^+$  denotes the set of positive integers. We further define a binary decision variable,  $Z_{ikl\theta}$ , where,  $i = 1, 2, \dots, n$ ;  $k = 1, 2, \dots, k_i$ ;  $l = f_1, f_2, \dots, f_L$ ; and  $\theta = 1, 2, \dots, m$ ; Here indices,  $i$ ,  $k$ ,  $l$ , and  $\theta$  denote task ID, corresponding version ID, viable frequency of the  $\theta$ -th processor and the processor ID, respectively.  $Z_{ikl\theta} = 1$ , if the  $k$ -th version of  $T_i$  (i.e.  $T_i^k$ ) executes on processor  $\theta$  at frequency  $f_l$ , otherwise 0. We define another binary variable  $Y_{ij}$ , where  $Y_{ij} = 1$ , if task  $T_i$  starts before  $T_j$ , else 0. If a



task  $T_i$  is executed with the  $k^{th}$  version at frequency level  $l$ , then its execution time will be denoted as  $ET(i, k, l)$ . We now present the objective function with constraints on the binary variables to model the scheduling problem.

**Maximise QoS** (1a)

$$QoS(\mathcal{A}) = \sum_{\theta=1}^m \sum_{i=1}^n \sum_{k=1}^{k_i} \sum_{l=f_1}^{f_L} Z_{ikl\theta} \times O_i^k \quad (1b)$$

**Subject to:**

$$\sum_{k=1}^{k_i} \sum_{l=f_1}^{f_L} \sum_{\theta=1}^m Z_{ikl\theta} = 1 \quad (1c)$$

$$S_n + \sum_{k=1}^{k_n} \sum_{l=f_1}^{f_L} \sum_{\theta=1}^m (ET(n, k, l) \times Z_{nkl\theta}) - 1 \leq D_{PTG} \quad (1d)$$

$$Pow_{peak} = \max\{Pow_{sys}\} \quad (1e)$$

$$Pow_{peak} \leq Pow_{BGT} \quad (1f)$$

$$\forall (\langle T_i, T_j \rangle) \in E, S_i + \sum_{k=1}^{k_i} \sum_{l=f_1}^{f_L} \sum_{\theta=1}^m ((ET(i, k, l) \times Z_{ikl\theta}) \leq S_j \quad (1g)$$

$$Y_{ij} + Y_{ji} > 0 \quad (1h)$$

$$Y_{ij} + Y_{ji} \leq 1 \quad (1i)$$

$$S_i + \sum_{k=1}^{k_i} \sum_{l=f_1}^{f_L} \sum_{\theta=1}^m ((ET(i, k, l) \times Z_{ikl\theta}) \leq S_j + (1 - Y_{ij}) \times \alpha \quad (1j)$$

Equation 1b presents the objective function in the above formulation, whereas Equation 1c enforces the constraint that each task  $T_i$  is assigned to exactly one processor with a particular version and executed at one frequency level. The application must meet its end-to-end absolute deadline  $D_{PTG}$ . Hence, the sink node  $T_n$  should be finished by  $D_{PTG}$ , which is represented by the constraint enforced in Equation 1d. The system-wide power constraint must be satisfied i.e. the peak power consumption of the defined system must not exceed the stipulated power budget. We represent the power constraints in Equation 1e and 1f, where  $Pow_{peak}$  represents the peak power consumption of the system. On the other hand,  $Pow_{sys}$  includes dynamic plus static power consumption of all the busy processors and is the summation of power consumption of all the tasks executing at that instant. Equation 1g, the precedence constraint between the tasks ( $T_i$  &  $T_j$ ), ensures that the execution of  $T_j$  should commence only after the completion of its predecessor  $T_i$ . Equation 1h to 1j represent the necessary constraints in order to avoid time-wise overlapping between tasks executing at the same processor. If tasks are executed in the opposite order, we use  $\alpha$  nullification to deactivate the constraint where,  $\alpha$  represents a large value.

### B. ARCTIC: Error Propagation

As per the ILP-based scheduling, when a task ( $T_i$ ) is scheduled with a lower version (assuming  $\zeta$ -th version, where  $1 < \zeta < k_i$ ), the result of a partially completed task shows

### Algorithm 1: Generating Schedule and V/F Readjustment

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**Input:**

- i. Task graph  $G(T, E)$
- ii.  $k_i$ : Number of versions of each task  $T_i$
- iii.  $len_i^j$ : Execution length of  $j^{th}$  version of task  $T_i$
- iv.  $D_{PTG}$ : The deadline of the task graph.
- v.  $Acc_i^j$ : accuracy achieved by executing  $j^{th}$  version of  $T_i$
- vi.  $F_l^j$ : implies a frequency level ( $l$ ) for processor  $j$ .

**Output:**

- i. Task Schedule /\* Selected Task versions ( $\zeta_i$ ), Execution start times ( $st_i$ ), Mapped Processor id: ( $P_i^j$  i.e.  $i^{th}$  task on  $j^{th}$  Processor, Obtained Accuracy) \*/
- ii. Achieved system-level QoS.

- 1 By considering all  $T_i \in T$  and all processors  $P$ , a schedule will be generated by employing the ILP given in Equation 1a to 1j, and this schedule is named as *PrimarySched*;
- 2 /\* Our ILP based scheduling mechanism will map the tasks to the cores and also selects the version of each task that will be executed. \*/
- 3 **for each**  $T_i \in T$  **do**
- 4     Generate the list of predecessor ( $PAR_i$ , list of predecessors for  $T_i$ ) for each of the  $|T| - 1$  tasks, as our single source task does not have any predecessor;
- 5     **if**  $T_i$  is not mapped/selected with its highest version **then**
- 6         Calculate  $OE_i$  and subsequently  $IE_i$  by employing Equation 2 and 3, respectively;
- 7         Derive  $EM_j$  for  $T_j$  through Equation 4, where  $T_j$  is a successor of  $T_i$ ;
- 8 By considering  $EM_i$  for each  $T_i$ , modify *PrimarySched*, and this modified schedule is named as *SchedMod*;
- 9 Let us assume task  $T_{\eta}^{P_j}$  is the last task scheduled at processor  $P_j$  ( $\forall P_j \in P$ ) in our schedule and one of such  $T_{\eta}^{P_j}$  will trivially be the sink task;
- 10 **if**  $\exists T_{\eta}^{P_j}$ , where  $FinishTime(T_{\eta}^{P_j}) > D_{PTG}$  **then**
- 11     *SchedNew* = Exploit\_Idle\_Slot(*SchedMod*) (Call Algorithm 2);
- 12     **if**  $T_{\eta}^{P_j} \in \text{SchedNew}$ ,  $FinishTime(T_{\eta}^{P_j}) \leq D_{PTG}$  **then**
- 13         *SchedFinal* = *SchedNew*;
- 14     **else**
- 15         Discard the schedule and return;
- 16 **else**
- 17     *SchedFinal* = *SchedMod*;
- 18 Store *SchedFinal* in dispatch table and return QoS;

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lower accuracy than the maximum possible value and this difference is termed output error ( $OE_i$ ) and is represented:

$$OE_i = O_i^{k_i} - O_i^{\zeta} \quad (2)$$

Since, the tasks ( $T_i$ ) are dependent, the error  $OE_i$  of  $T_i$  is propagated to its successor task(s), in terms of extra computational cycles. Hence, the additional cycles ( $IE_i$ ) of a task ( $T_i$ ), due to propagated errors by its predecessor(s) can be defined as:

$$IE_i = \sum_{p=1}^{PAR} OE_p \quad (3)$$

where  $PAR$  is the number of predecessors of  $T_i$ . This propagated error extends the mandatory part of the successor ( $T_j$ ), since more processor-cycles are needed by the task to process the error. The extended mandatory part of a task ( $T_j$ ) can be expressed as:

$$EM_j = M_j + IE_i \quad (4)$$

### C. Generating Schedule and V/F Readjustment

The scheduling process of ARCTIC-Offline is given in Algorithm 1. The task graph ( $G(T, E)$ ), in addition with the individual task's versions ( $k_i$ ), execution lengths ( $len_i^j$ ) and deadline ( $D_{PTG}$ ) are the inputs to this algorithm. The algorithm also considers  $Acc_i^j$  and  $F_i^j$  as inputs, which are the accuracy achieved by executing the  $j^{th}$  version of  $T_i$  at a frequency level of  $L$  for processor  $j$ . With the onset of the schedule generation process, Algorithm 1 employs the ILP based scheduling discussed in Sec. IV-A (line 2). The ILP considers power, precedence and time constraints and available cores to generate the primary schedule, *PrimarySched*. The generated schedule might not be able to execute all the tasks with their highest versions. By considering that schedule,  $OE_i$  for individual  $T_i$  is generated next and subsequently  $IE_i$  will be derived by employing Equation 2 and 3, before deriving  $EM_j$  by employing Equation 4. To generate  $EM_j$ , the list of predecessor for all tasks are also considered. The entire process of generating  $EM_j$  is written in line 3 to 7.

Once the extended mandatory part is generated ( $EM_j$ ), the *PrimarySched* is next modified and this schedule is named *SchedMod* (line 8). As *SchedMod* is burdened with additional execution cycles, this might result in a violated deadline. Any task  $T_\eta$ , the last task (can potentially be the sink task) that has been scheduled on processor  $P_j$  ( $T_\eta^{P_j}$ ) and having its finish time after the deadline, i.e.  $FinishTime(T_\eta^{P_j}) > D_{PTG}$ , trivially implies that the deadline is violated (line 10). Upon detection of such deadline violation, Algorithm 2 will be called (line 11), where existing possible idle slots at some cores will be exploited as much as possible to adjust the frequency of the non-idle cores by respecting power constraints.

To update the *SchedMod*, Algorithm 2 first considers the tasks scheduled at each processor ( $P_i$ ). Now, for each  $P_i$ , Algorithm 2 detects the idle slots by considering finish time and start time of two subsequent tasks (line 1 to 5). For each such idle slots at a particular processor ( $P_i$ ), Algorithm 2 searches if any other processor(s) ( $P_j$ ) is scheduled with a lower frequency, (where  $P_i \neq P_j$ ), then the frequency of  $P_j$  is set at the highest level for that slot (line 6 to 8). Such overlap slots between a pair of processor cores are detected by listing the idle slots of each individual processors ( $IdleSlots(P_i)$ ). For such individual idle slots of a particular processor ( $P_i$ ), all other processors' schedules will be verified and the active-idle overlap pairs will be detected accordingly. However, such changes in frequency will reduce the execution lengths of the individual tasks, for which *SchedMod* will be updated and the updated schedule is named as *SchedUpdate*, which is next returned to Algorithm 1 (line 9 to 10 in Algorithm 2). Upon receiving the updated schedule, Algorithm 1 checks if this new schedule is meeting the deadline (line 12). If a new schedule meets its deadline, Algorithm 1 stores this final schedule *SchedFinal* in dispatch table and returns the QoS (line 17). Otherwise, the schedule will be discarded (line 15).

### D. Example: Constrained scheduling at work

By applying the ILP based mechanism for the proposed scheduling problem based on the PTG depicted in Figure 2,

### Algorithm 2: Exploit\_Idle\_Slots (*SchedMod*)

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1 for each processor ( $P_i$ ) do
2   List the tasks scheduled at  $P_i$  by considering SchedMod ;
3   for each pair of subsequent tasks ( $T_i, T_j$ ) do
4     if  $StartTime(T_j) > FinishTime(T_i)$  then
5        $IdleSlots(P_i)[] = \{StartTime(T_j) - FinishTime(T_i)\}$  ;
6 for each entry in  $IdleSlots(P_i)[]$  do
7   if  $P_j$  is scheduled with lower frequency, where  $P_i \neq P_j$  then
8     Set the frequency ( $F_i^j$ ) at the highest level for  $P_j$  ;
9 Re-calculate the time-stamps and spans for each task in SchedMod
  along with its successors, for which frequency has been readjusted,
  and the new schedule is named as SchedUpdate ;
10 Return SchedUpdate ;

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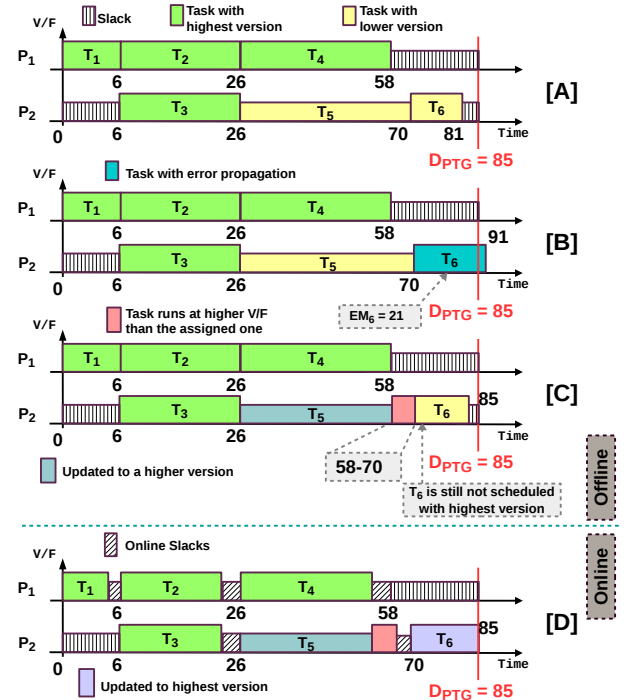


Fig. 3: Generated Schedule and V/F readjustment, and online LLC induced improvement (not to scale).

Algorithm 1 at first generates the *PrimarySched* as shown in diagram [A] of Figure 3, whereas our assumed system has two processors ( $P_1$  and  $P_2$ ) and with an overall power-budget of 35 units.

Note that, the source task does not have any such overhead. In Figure 3,  $T_5$  is scheduled with a lower version, hence  $T_6$  will be scheduled with an extended mandatory part  $EM_6$  as shown in diagram [B], which is the modified schedule, *SchedMod*, derived by Algorithm 2. Such error propagation leads to deadline violation for *SchedMod*, which is shown in diagram [B] of Figure 3.

The assigned V/F levels of a processor is adjusted by observing the assigned V/F level of the other processor(s) so that the power constraint is not violated. During task-allocation, the V/F level for each task on a specific processor is determined. For a pair of processors, if there exist any overlapped time-slots where one processor is idle, and the other one is executing a task at some lower V/F, then ARCTIC

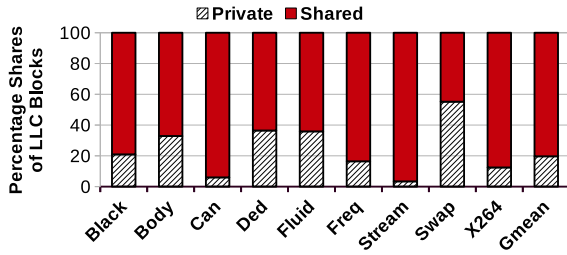


Fig. 4: Percentage shares of Private and Shared LLC Blocks. will increase V/F of that processor (shown in Figure 3[C]). Note that, this task-level V/F readjustment will reduce the execution length of tasks, and thus will improve the QoS. In Figure 3[C], our *SchedFinal* is depicted, in which the V/F adjustment reduces the execution length of the task  $T_5$  in diagram [B]. Hence, completion time of  $T_5$  remains same at 70, however, a higher version has been scheduled, thanks to V/F adjustment. Even after scheduling a higher version of  $T_5$ ,  $T_6$  can also be completed without a deadline-violation and our final obtained QoS is 46 (Figure 3[C]). The feasible schedule, *SchedFinal* is next stored into the dispatch table [28] by Algorithm 1, and subsequently, the tasks will be executed.

## V. ARCTIC-Online

In this section, we will illustrate the ARCTIC-Online mechanism after discussing the background on private blocks. Basically, the schedule generated by Algorithm 1 is deployed for execution and the online mechanism attempts to improve QoS and energy efficiency.

### A. Analysing Exclusive Cache Blocks

To analyse the presence of shared and private blocks in the LLC, we executed a set of PARSEC benchmarks [10] in gem5 [11]. The footprints of private and shared blocks have been captured once the execution of an application proceeds to the region of interest (ROI). The traces have been captured at the end of each million of clock cycles, and we took this traces for 80 million clock cycles within the ROI<sup>1</sup>. The percentages of private and shared LLC blocks are shown in Figure 4. Our analysis shows, on average, about 20% of all LLC blocks are private, and can be as high as 58% for some applications (e.g., *Swap*). As we consider an inclusive cache hierarchy, a significant LLC-space is occupied by the private blocks. However, a single copy of such exclusive cache blocks in the respective requester cores' private caches can maintain the functional correctness and thus a large portion of the LLC will be freed up, which can be filled up by more live blocks to improve performance.

In case of an exclusive cache hierarchy, the effective cache capacity is significantly higher than the inclusive ones. But, maintaining coherency at the shared cache in exclusive cache hierarchy can incur significant costs in terms of latency and energy usages [47]. Implementation of coherence state machine for the exclusive cache hierarchy is more complex than

its inclusive counterparts, and exclusive cache also requires an additional victim buffer, which will further incur extra area as well as energy overhead. While considering the sharing pattern between blocks as shown in Figure 4, it can be stated that, the larger percentage of the LLC blocks are shared in nature. Hence, implementing exclusive cache hierarchy can incur significant energy, area and coherence overheads [19], [20]. In ARCTIC-Online, we therefore propose an inclusive cache hierarchy with slight modification in the coherence management scheme, that will handle the private blocks like an exclusive cache, while shared blocks will be handled normally like the inclusive cache. Such technique will not incur energy, area, coherence or implementation overheads like exclusive cache, but can exploit the benefits of the exclusive cache for the private blocks.

### B. Core Concept of ARCTIC-Online

The entire mechanism of ARCTIC-Online is governed by Algorithm 3. This algorithm handles LLC management (described in Sec. V-B1) techniques along with the online QoS improvement and energy savings. Time span between the starting time till deadline is called *Frame*, within which the scheduled tasks need to be executed. The tasks are fetched from the dispatch table for execution (line 3), and while executing the tasks, the LLC management algorithm (Algorithm 4) is executed at each LLC bank simultaneously (line 5 to 7). On the other hand, the core based QoS improvement and energy savings are also handled at each core simultaneously (line 8 to 10) by employing Algorithm 8 (discussed in Sec. V-B2).

#### Algorithm 3: ARCTIC-Online Mechanism

```

1 for each Frame do
2   for all  $T_i$  in Dispatch Table do
3     Get schedule details of each  $T_i$  from the Dispatch Table;
4     Fetch  $T_i$  and start execution;
5     for each LLC bank do
6       Call Algorithm 4;
7       # Execute simultaneously at each bank;
8     for each Core do
9       Call Algorithm 8;
10      # Execute simultaneously at each core;
```

1) *Managing LLC Blocks*: To maintain a single copy of the private cache blocks in the inclusive cache hierarchy, the coherence protocol must be updated to ensure functional correctness. In ARCTIC-Online, the allocation will be performed in the following manner. We have segregated three cases for managing coherency in ARCTIC-Online, and the sequence of operations for each one is shown in Figure 5, whereas the whole implementation framework is given in Algorithm 4. In case [A] in Figure 5, once a miss is detected at both L1-D ① and LLC ② (line 3 in Algorithm 4), the request will be sent to the main memory (line 4) and an entry will be created in the directory (line 5). Upon receiving the memory response (line 11 to 12), the associated request type (read/write) and the number of requester(s) will be determined, the response management framework is detailed in Algorithm 7. When a miss is detected at the local data cache, but the data is

<sup>1</sup>By evaluating LLC traces for longer time-span (of 200 million clock cycles), we observed that the shares of private and shared blocks does not change significantly. Hence, we decided to take the values derived at the 80 million clock cycles.





**Algorithm 6: Handling NT Hit**


---

```

1 if (Req.type == Wr_Req) or ((Req.type == Rd_Req) and
  (C_D.sharer == 1)) then
2   # Send Invalidation to all the sharer(s) and send block to the
   Req.ID;
3   # Reset Sharer list in C_D and initialize owner entry with
   Req.ID;
4   # Migrate the NT.tag from NT to DLT;
5   # C_D.state = E_P;
6 if Req.type == Last_PUTS then
7   # Reset Sharer list in C_D;
8   # C_D.state = U;
9 else
10  if (Req.type == Rd_Req) and (C_D.sharer > 1) then
11    # Serve the Req from NT;
12    # Add Req.ID in C_D sharer list;
13    # C_D.state remains S;

```

---

**Algorithm 7: Handling Response from Main Memory**


---

```

1 if (Resp.type == Wr_Req) or ((Resp.type == Rd_Req) and
  (#Req.ID == 1)) then
2   # Allocate Data less entry in DLT;
3   # Send Resp.Data to requester local cache;
4   # Create C_D with owner entry set to requester local cache ID;
5   # C_D.state = E_P;
6 else
7   if (Resp.type == Rd_Req) and (#Req.ID > 1) then
8     # Allocate Resp.tag and Resp.Data in LLC NT;
9     # Serve the Resp.Data to requester local caches;
10    # Create C_D with sharers list initialized to requester
      cache IDs;
11    # C_D.state = S;

```

---

If a shared block is evicted from all of its sharers' L1s (*Last\_PutS*), the state is changed to *U* from *S* (line 6 to 8). Upon receiving a read request for a shared block having more than one sharer (line 10), the request is served from NT with updating the sharers' list in the directory and the coherence state will remain the same at *S* (line 11 to 13). The respective transitions of the coherence states are depicted in Figure 6.

**Handling Response from Memory (Algorithm 7):** In case of an exclusive-read (having single requester) or a write LLC miss, the data is directly sent to the requester's data cache upon receiving the response from the main memory. The coherence state of the data is directly made as *E\_P* by creating an entry in the DLT with updating the owner of the block (line 1 to 5). In case of a read LLC miss, while having multiple requester cores, the tag and data are allocated in the LLC's data array and NT array, and the copies of the data will be sent to the requester cores' local cache after updating the sharers' list in the coherence directory and setting the coherence state as *S* (line 7 to 11). The detailed coherence state transitions are given in Figure 6.

### 2) Improving QoS & Energy Efficiency (Algorithm 8):

By maintaining exclusive cache entries for the private blocks, ARCTIC-Online frees up empty LLC spaces, that are further used to increase live block count. Such mechanism minimises LLC misses, which improves performance of the tasks and reduces the execution time of the individual tasks. After executing the mandatory portion ( $M_i$ ) of the individual tasks, ARCTIC-Online evaluates its remaining time for executing the task (line 1 to 3). To calculate remaining execution

**Algorithm 8: Improving QoS and Energy Efficiency**


---

```

Input: Break_Even_Time
1 # Execute  $M_i$  as per schedule ;
2 if Execution of  $M_i$  is over then
3    $Cyc\_rem_{O_i} = (Cyc\_Ext\_End_{T_i} - Cyc\_End_{M_i})$  ;
4 if Highest  $O_i$  is not scheduled then
5   # Call the function that returns optional part with highest
     possible accuracy which can run within  $Cyc\_rem_{O_i}$  ;
6    $O_i = get\_O_i(T_i, Cyc\_rem_{O_i})$  ;
7   if  $O_i$  then
8     #Fetch the  $O_i$  ;
9 if Execution of  $T_i$  is over then
10   $Slack\_after_{T_i} = (Cyc\_Ext\_End_{T_i} - Cyc\_End_{T_i})$  ;
11 if  $Slack\_after_{T_i} > Break\_Even\_Time$  then
12  #Power gate the core ;
13 if Core is power gated then
14   $Slack\_after_{T_i}--$ ;
15  if  $Slack\_after_{T_i} == Break\_Even\_Time$  then
16    #Turn on the core ;

```

---

time ( $Cyc\_rem_{O_i}$ ) for each task, we introduced extended end time of each task ( $Cyc\_Ext\_End_{T_i}$ ), which is defined as follows.  $Cyc\_Ext\_End_{T_i}$  for  $T_i$  is set as the starting time either of the next task at the same core or of its successor task, whichever is earlier. If  $T_i$  is a sink task, then  $Cyc\_Ext\_End_{T_i}$  is set at  $D_{PTG}$ . However,  $Cyc\_rem_{O_i}$  is calculated by considering the time-span between the current time-stamp (at the end of  $M_i$ ) and  $Cyc\_Ext\_End_{T_i}$ . If the highest version of the task is not scheduled,  $Cyc\_rem_{O_i}$  is used to decide if a higher version of the task can be executed, subject to availability (line 4 to 6). Otherwise, the task version will remain unchanged, i.e. the scheduled  $O_i$  will be executed (line 7 to 8). This will assist in improving overall QoS during task execution. However, as execution time of the  $O_i$  will also be minimised due to cache based performance improvement of ARCTIC-Online, there is a chance of generating dynamic slack after execution of each task. If such slack exists and its span (evaluated at line 11 to 12) is more than break even time of the respective processor core, the core will be shutdown for energy saving, and will be turned on before starting-time of the next task (line 13 to 16).

### 3) ARCTIC: Online Computational Overhead:

**Theorem 1.** The amortized complexity of ARCTIC-Online (Algorithm 3 to 8) is  $\frac{\mathcal{O}(n \cdot k)}{D_{PTG}}$  per time-slot.

*Proof.* Algorithm 3 is the master algorithm of ARCTIC-Online technique that executes tasks at each core. A step-wise analysis of computational overhead of Algorithm 3 due to the called functions/algorithms is as follows:

- 1) The “for loop” from line 2 to 10 may be executed  $\mathcal{O}(n)$  times in the worst-case, although the number of tasks assigned to a core usually takes a small value.
- 2) Next, the “for loop” from line 5 to 7 will be executed in constant time, as the number of LLC bank is always constant.
  - Algorithm 4 to 7 are called next during task execution. For all practical purposes, computational overheads of these algorithms may be considered to be constant, however, implementation overheads for Algorithm 5 and 7 is discussed in Sec. V-B4.



- 3) The “for loop” from line 8 to 10 will be executed in constant time, as the core count is always constant.
  - In worst-case, for Algorithm 8, the loop will execute line 4 to 8 which can have a worst-case complexity of  $\mathcal{O}(k)$ , where  $k$  is the maximum number of versions for a task  $T_i$ .
- 4) Hence, the worst-case computational complexity of Algorithm 3 is  $\mathcal{O}(n \cdot k)$ .
- 5) At any *FRAME*, the total overhead for generating the schedules over all processor cores for the duration of a *FRAME* is  $\mathcal{O}(n \cdot k)$  in the worst case.
- 6) As the *FRAME* length is in  $\mathcal{O}(D_{PTG})$ , the amortized complexity of ARCTIC: *Online* is  $\frac{\mathcal{O}(n \cdot k)}{\mathcal{O}(D_{PTG})}$ .  $\square$

4) *Implementation Overhead*: The implementation of ARCTIC-*Online* requires additional tag entries at the LLC, called DLT, for bookkeeping the tag and coherence states of the private blocks. Each LLC tag entry will be equipped with DLT space, which will be filled up with the tag entries of the blocks having the same index. We analysed the power and area overheads for adding 25% and 50% extra tags for implementing DLT and corresponding area and power overheads have been analysed with FinCanon [26] by considering a 14 nm FinFET technology. With 25% (50%) extra tag, LLC will experience an area overhead of 2.32% (4.53%), with a power overhead of 2.71% (5.64%). The power and area overheads are not significant, due to lower leakage consumption and higher cell-density of the FinFET-based caches [26]. To implement Algorithm 8, the per-core power gating (PCPG) technique can be employed at the circuit level, which does not incur any significant circuit overhead [27].

## VI. EVALUATION

In this section, we first showcase the efficacy of ARCTIC-*Offline*, followed by the evaluation of ARCTIC-*Online*, and show how ARCTIC improves system level QoS.

### A. Methodology

1) *ARCTIC-Offline*: We define **Normalized Obtained QoS** (NOQ) as the ratio between the actually achieved QoS for the PTG, and the maximum achievable QoS by executing the highest versions of all tasks. NOQ can be formulated as:  $NOQ = \frac{\sum_{i=1}^n Acc_i^j}{\sum_{i=1}^n Acc_i^{k_i}}$ , where  $k_i$  represents the highest version of task  $T_i$ . Next, we model our multi-core and the task-set:

- *Processor System*: A homogeneous multi-core platform having 4 Intel x86 cores (i.e.,  $m = 4$ ) has been considered. The TDP of the individual cores are scaled and set as 10.5W, by considering the Intel Xeon’s data-sheet [1]. The runtime core power is obtained through McPAT [29].
- *Task-set*: Task characteristics have been taken from a prior technique, *Prepare* [13], where tasks are framed by using PARSEC benchmark applications. The total execution requirement of a PTG ( $C_{PTG}$ ) is the sum of the execution times of its subtasks,  $C_{PTG} = \sum_{i=1}^n ET_i$ . Thus, utilization  $U_i$  of a PTG can be written as  $\frac{C_{PTG}}{D_{PTG}}$ .

TABLE I: System parameters [CC: clock cycle]

Parameter	Value	Parameter	Value
ISA	Intel x86	L1-I	64KB, 4Way, 3CC
#Cores (type)	8 (Xeon)	L1-D	64KB, 4Way, 3CC
Max. V/F (Max_VF)	1.12V, 3.0GHz	L2	8MB, 16Way, 12CC
Min. V/F (Min_VF)	0.6V, 1.5GHz	Cache	Non-MRU, 64B blocks
Power_gate_overhead	60 ns	DRAM latency	70 ns
ROB Size	200	Technology	14 nm FinFET
Dispatch/Issue width	8	Ambient Temp.	47 °C

The average utilization of a PTG is taken from a normal distribution, by considering a normalized frequency of 0.6. Given the PTG’s utilization, we next obtain the total utilization of the system ( $Sys_{uti}$ ) by summing up the utilization of all PTGs. Given the  $Sys_{uti}$ , the total system workload ( $Sys_{WL}$ ) / system pressure can be obtained by:  $Sys_{WL} = \frac{Sys_{uti}}{m}$ . For a given  $Sys_{uti}$ , we generated all of our PTGs by following the method proposed in *Prepare* [13]. Given a  $Sys_{WL}$ , a set of PTGs are created. The number of PTGs ( $\rho$ ) within a set is calculated as:  $\rho = \frac{m \times Sys_{WL}}{U_i}$ . In our generated PTGs, the minimum number of tasks is 5 and the maximum number of tasks is 20. For each PTG in the set, the number of tasks are generated randomly within a preset limit. Note that, as the individual  $U_i$  of a PTG is lower than the given  $Sys_{WL}$ , the number of PTGs ( $\rho$ ) within the set will always be higher than  $m$ .

- *Task Temporal Parameters*: For each  $T_i$ , based on which portion of the  $len_i$  is considered as the mandatory portion ( $M_i$ ), the following cases are considered [21]: (i) *man\_low* :  $M_i \sim U(0.2, 0.4) \times len_i$  (low portion of a task  $T_i$ ’s length ( $len_i$ ) is for the mandatory portion). (ii) *man\_med* :  $M_i \sim U(0.4, 0.6) \times len_i$  (medium portion of a task  $T_i$ ’s length ( $len_i$ ) is for the mandatory portion). (iii) *man\_high* :  $M_i \sim U(0.6, 0.8) \times len_i$  (high portion of a task  $T_i$ ’s length ( $len_i$ ) is for the mandatory portion).

2) *ARCTIC-Online: Simulation Infrastructure*: In this work, we simulated a homogeneous CMP, having 8 Intel x86 Xeon OoO cores in the gem5 full system simulator [11]. Each core is equipped with its private L1 data and instruction caches. The L2 cache, considered as LLC, is logically shared among the cores. The performance traces derived from gem5 are sent to McPAT-Monolithic [23], to generate the power traces, and system parameters used in the simulations by considering 14nm FinFET technology nodes are listed in Table I. In our simulation framework, each core can execute tasks either at Max\_VF (3.0GHz) or at Min\_VF (1.5GHz). By considering prior arts, where PARSEC [10] can be used in an approximate computing based paradigm [2], [42], we framed our task-set by defining each task with 4 PARSEC applications with large input sets. We constructed each  $M_i$  and  $O_i$  by using two copies of two different PARSEC applications, where the execution lengths of  $M_i$  and  $O_i$  for each task are set by scaling each values of  $M_i$  and  $O_i$  of Figure 2 with 20M clock cycles. Our multi-programmed task-set is detailed in Table II, where the execution lengths (EL) are given in millions of cycles in the region of interest (RoI) for the respective  $M_i$ ’s and  $O_i$ ’s. Each task’s  $M_i$  and  $O_i$  run on a group of 4 cores, and we consider two such groups to represent  $P_i$  in Figure 3.

TABLE II: Tasks formation with PARSEC [10], [39]. *Black* (2) implies two copies of *Black*, which is the same for others. (Acronyms: Blackscholes (*Black*), Bodytrack (*Body*), Canneal (*Can*), Dedup (*Ded*), Fluidanimate (*Fluid*), Freqmine (*Freq*), Streamcluster (*Stream*), and X264 (*X264*)). The execution lengths (ELs) are in million cycles.

Tasks	Benchmarks ( $M_i, O_i$ )	EL ( $[M_i], [O_i]$ )	Sel. $O_i$ [EL]
$T_1$	<i>Black</i> (2), <i>Body</i> (2)	[80], [40]	#1 [40]
$T_2$	<i>Stream</i> (2), <i>Swap</i> (2)	[200], [100, 160, 200]	#2 [200]
$T_3$	<i>Ded</i> (2), <i>Can</i> (2)	[200], [100, 140, 200]	#3 [200]
$T_4$	<i>X264</i> (2), <i>Fluid</i> (2)	[400], [140, 240]	#2 [240]
$T_5$	<i>Freq</i> (2), <i>Swap</i> (2)	[340], [100, 220, 300]	#2 [220]
$T_6$	<i>Ded</i> (2), <i>Body</i> (2)	[200], [20, 120]	#2 [20]

### B. ARCTIC-Offline

ARCTIC-Offline is evaluated based on task rejection rate (*TRR*), which is the ratio of the number of tasks that did not finish their execution within their deadline, over the number of all tasks executed by the system. We obtain task characteristics and the total utilization of the system ( $Sys_{uti}$ ) from a prior art, proposed by S. Saha et al. [39]. The left plot in Figure 7 depicts the *TRR* obtained by ARCTIC-Offline for 40, 60 and 80% of  $Sys_{WL}$ . We observed that *TRR* remains 8%, when the system workload is low, which is increased to 35% on average, when the workload is scaled up by 40%. As the system workload is increased to maintain the number of PTGs in the system, the individual PTG-utilization also increases, that eventually contributes to high *TRR*. Actually, increased utilization results in longer running time of each node, that trims the possibility of obtaining sufficient free slots within the deadline. Moreover, the insufficient free slots curtail the chances of selecting higher task versions, thus increase in the error propagation. This cascading effect increases the execution length of the sink node that violates the deadline.

In case of  $man_{high}$ , the *TRR* increases in a lower rate than for  $man_{med}$  and  $man_{low}$ , while increasing  $Sys_{WL}$  (shown in Figure 7 (Left)). Basically, when mandatory portions of the individual tasks are high, the length of the optional portions will be low, that results into lower variance among the different versions of a task, which reduces error propagation.

The right plot in Figure 7 shows the reduction in *TRR* (*RTRR*) for different values of  $Sys_{WL}$ . We compared the changes in *RTRR* for ARCTIC-Offline (suffixed by \_AR) with the scheduling proposed in *TD* [36] (suffixed by \_TD). We observed that, increased  $Sys_{WL}$  trivially reduces *RTRR* for ARCTIC-Offline, which still significantly outperforms *TD* for all the workloads. This is because *TD* accounted no power-budget, whereas the assumed energy budget increased with higher number of tasks. Moreover, *TD* also allows unlimited task migration that incurs extra overheads. For a given  $Sys_{WL}$ ,  $man_{low}$  obtains a higher reduction in *TRR*, as the lengths of the mandatory (optional) parts of individual tasks are short (long), that also increases the probability of obtaining slacks.

We have compared our policy with a prior strategy (*SENAS*) [22] and the results are shown in Figure 8 in case of  $man_{med}$ . For a fair comparison with *SENAS*, we firstly derived the overall energy limit based on our considered power budget ( $Pow_{BGT}$ ) of ARCTIC's experimental framework. The

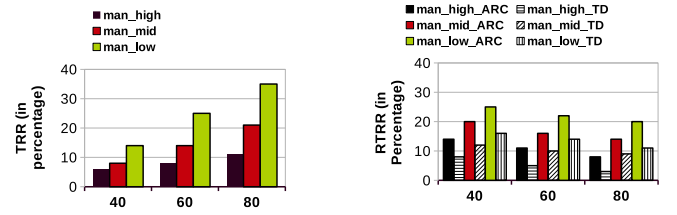


Fig. 7: System Workload (in percentage) vs. TRR (Left), and RTRR (Right).

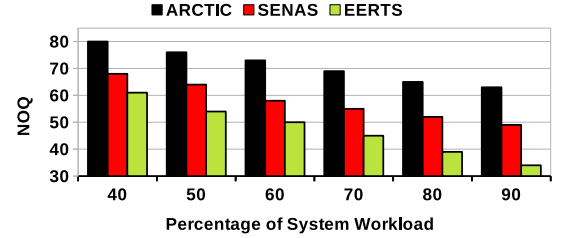


Fig. 8: Comparing NOQ: ARCTIC vs. Prior arts.

same value is used as energy budget for *SENAS* as well. It can be observed, as the number of task increases (due to increase in  $Sys_{WL}$ ), that ARCTIC maintains higher QoS by achieving higher NOQ than *SENAS*. ARCTIC is able to maintain close to 70% QoS with 70% workload, where *SENAS* achieves 55% QoS. This is because *SENAS* did not consider any power limits but assumed a fixed energy budget. Moreover, *SENAS* assumed that the task's energy consumption increases with its execution cycle, i.e., the higher the task's execution, the higher the energy requirement. Hence, for a fixed energy budget, *SENAS* fails to execute tasks with a higher version and thus, ends up with a lower QoS.

We compared our offline strategy also with EERTS [8] and it can be observed from the figure that EERTS achieved considerable NOQ with low system utilization. However, NOQ decreased significantly with the increase in system workload. This is mainly due to the fact that EERTS only considered tasks with a linear task chain and considered only the latency constraint but not the power budget has been considered. Now, when the system workload is low, the utilization of individual tasks is also low, and this correspondingly attributes to a lower number of tasks/nodes within a graph (Sec. VI-A). Thus EERTS achieved close to 60% NOQ. However, as the workload increases, the number of nodes also increases, making the graph structure more skewed. Hence, EERTS fails to achieve a higher QoS, as tasks with a higher versions cannot be scheduled due to stringent power, resource and deadline constraints.

### C. ARCTIC-Online

1) *Performance Improvement and EDP gains*: We first evaluate the reduction in LLC misses (MPKI), and the IPC values for each task, with two different extra DLT storage of 25% (ARC\_25) and 50% (ARC\_50). We also compare these results with a prior LLC way-sharing and way-gating based technique, *ACCURATE* [39] (ACCRT), the results for MPKI reductions are shown in Figure 9 for all tasks. For  $T_3$

and  $T_4$ , the higher number of shared LLC blocks curtails the benefits of ARCTIC-Online, whereas for  $T_2$ ,  $T_5$  and  $T_6$  higher private block counts lead to significant reduction in MPKI. The MPKI reduction is higher in ARC\_50 than ARC\_25, due to accumulation of more live blocks. For tasks like  $T_3$ , having higher private block count during  $M_i$  and higher shared blocks during  $O_i$ , the performance improves further during  $M_i$  than during  $O_i$ , thus the slack-span is getting longer. On the other hand,  $T_4$  contains higher shared block counts during  $M_i$ , which lowers the performance benefits during  $M_i$ . For all tasks, ACCRT achieves lower reduction in MPKI (9.4% on average) than both ARC\_25 (13.5% on average) and ARC\_50 (30.2% on average), as ACCRT turns off some portions of the LLC to reduce LLC leakage. However, this lower MPKI reduction leads to lower IPC improvement (2.7% on average) for ACCRT whereas ARC\_25 and ARC\_50 achieve 5.2% and 8.9% average improvements in IPC, respectively. Figure 10 shows the IPC improvements for all of our tasks for ARCTIC-Online and ACCRT. The higher the number of private blocks during both  $M_i$  and  $O_i$  in case of  $T_6$  the more significant reduction in IPC, that enables to enhance QoS by executing higher version of  $O_i$ . For all tasks, ARC\_50 reduces more MPKI during  $M_i$  than ARC\_25, which generates longer slack in ARC\_50, which in turn leads to higher energy savings. For individual tasks, we evaluated the EDP gains for ARCTIC-Online and ACCRT, as shown in Figure 11. The average EDP gains for both ARC\_25 and ARC\_50 are around 5.3% and 9.1%, respectively, that surpass the EDP gains of 2.7% for ACCRT. ARCTIC-Online power gates the cores for a sufficiently longer time-span during its longer slacks, that in turn leads to higher EDP gain.

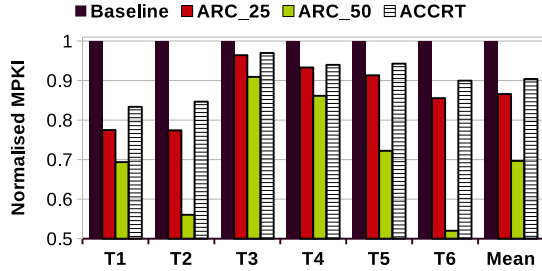


Fig. 9: Normalised MPKI.

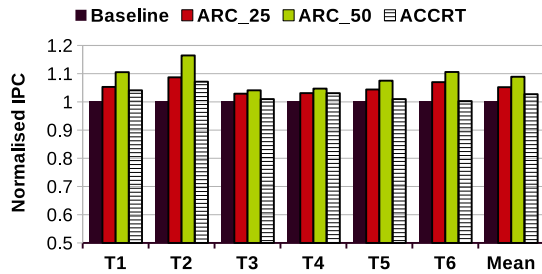


Fig. 10: Normalised IPC.

Figure 12 shows how ARCTIC-Online improves the QoS and energy efficiency by reducing execution length of the

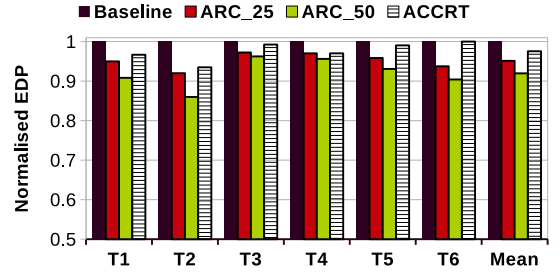


Fig. 11: Normalised EDP.

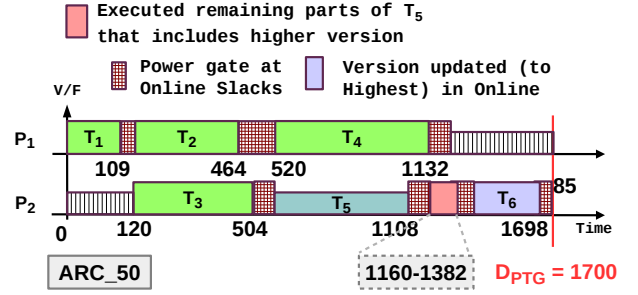


Fig. 12: QoS Update in Online for ARC\_50. Timeline is based on Table II.

tasks, while applying ARC\_50. ARCTIC-Online reduces the execution lengths of individual tasks, that generates slacks at the end of each task, during which cores are power gated to save energy. For all but sink tasks, starting time-stamps are kept the same, as derived by ARCTIC-Offline. However, once all predecessor tasks are completed, ARCTIC-Online schedules the sink ( $T_6$ ) and based on the available time-span and the highest possible version of  $O_i$  is executed. In ARC\_50, ARCTIC-Online executed the highest version of  $T_6$ , that improves QoS by 10%, with an overall energy saving of 6.21%, even after exploiting the slack. However, in ARC\_25, the online QoS improvement is 4% with 12.32% energy saving, as  $T_6$  is able to execute its second version within deadline. However, higher IPC improvements for all tasks in ARC\_50 generate longer slacks, which are exploited to save more energy.

TABLE III: Outputs of ARCTIC-Online

Tasks	Mapped Core	Final Version	Amount of Slack (over Offline)
$T_1$	$P_1$	1	9.2%
$T_2$	$P_1$	3	14.0%
$T_3$	$P_2$	3	3.8%
$T_4$	$P_1$	2	4.4%
$T_5$	$P_2$	2	6.9%
$T_6$	$P_2$	2	9.6%
Improvement in Achieved QoS			10.0%

#### D. Discussion: Applicability of ARCTIC in Heterogeneous Platform

To showcase the efficacy of ARCTIC-Online while employed in heterogeneous platforms, we further evaluated both ARC\_25 and ARC\_50 of ARCTIC-Online in our simulation



TABLE IV: Heterogenous System parameters [CC: clock cycle]

Parameters		Values
Big Core	ISA	RISC-V (RV64GC)
	Cores	4 cores, single issue, in-order
Tiny Core	L1 Cache	4KB L1/D, 2-way, 1 CC
	Cores	RISC-V (RV64GC)
Tiny Core	L1 Cache	60 cores, 4-way out of order
	L1 Cache	16 entry LSQ, 128 entry ROB
L2 Cache		64KB L1/D, 2-way, 1 CC
		Shared, 8-banks, 1MB per bank,
Network		8-way, 1 bank per mesh column
		8x8 mesh, XY routing, 16B per flit
Benchmark Suite: Ligra [41]		BC, BF, BFS, BFS-BV,
		CC, MIS, RADII and TC

infrastructure. We model heterogeneous multi-core system in gem5 [11], with different core types, e.g. Big-core and Tiny-core, employing the setup proposed by Wang et al. [45]. Table IV details the system parameters used for our heterogeneous simulation. In the simulated system, each core has its own private L1 data and instruction caches and all cores share the L2 cache, which is considered as LLC. Due to existing limitations related to support-ability of PARSEC benchmark applications in heterogeneous simulation infrastructure of gem5, we used Ligra benchmark suite [41], which is also used to construct task-sets in approximate computing paradigm [44]. The applications chosen for evaluation are also listed in Table IV.

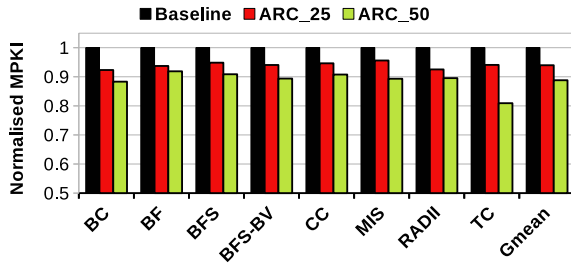


Fig. 13: Normalised MPKI: in Heterogeneous Multicore.

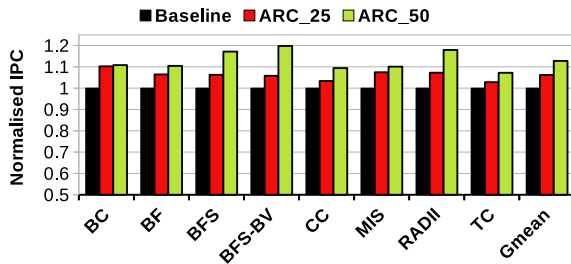


Fig. 14: Normalised IPC: in Heterogeneous Multicore.

Our evaluation shows, for all applications, *ARC\_50* shows higher reduction in MPKI than *ARC\_25*, as we have seen in case of homogeneous system. The MPKI reduction for all applications are plotted in Figure 13. Overall, MPKI across all applications is reduced upto 8% and 12% for *ARC\_25* and *ARC\_50*, respectively, over the baseline, whereas the respective average values for *ARC\_25* and *ARC\_50* are 6%

and 11%. This reduction in MPKI further leads to performance improvement, which is shown in Figure 14, by plotting results for IPC. For all applications, the average IPC improvement is 6% and 13% for *ARC\_25* and *ARC\_50*, respectively, whereas the respective ranges for IPC improvements for *ARC\_25* and *ARC\_50* are in 2-10% and 7-20%. This significant reduction in MPKI and IPC improvement in case of heterogeneous system demonstrates that ARCTIC can also be a promising technique in heterogeneous systems to stimulate QoS of an approximate real-time computing paradigm.

## VII. CONCLUSIONS

In ARCTIC, we introduce a novel hybrid offline-online *scheduling strategy* for approximate real-time tasks. ARCTIC generates a schedule for a dependent task-set with an objective to maximise the QoS while respecting other system-wide constraints. ARCTIC-Offline further considers the tasks scheduled with lower accuracy and schedules the portions of their respective optional parts with their respective successors, known as Error Propagation. As Error Propagation might lead to deadline violation, ARCTIC-Offline also introduced a V/F readjustment technique at the task level granularity, while respecting the power budget and deadline. At runtime, ARCTIC-Online keeps the only copies of the private blocks in the respective local caches, and frees up the LLC locations. These spare LLC spaces are further utilized to boost performance by accumulating more live blocks on-chip, reducing tasks' execution-times. The slacks generated by reduced execution-time will further be exploited to enhance QoS by executing more from the tasks' optional parts or improve energy efficiency by power gating the core. Simulation results show that, for a set of tasks ARCTIC-Offline reduces task rejection rate up to 25%, whereas ARCTIC-Online yet improves QoS by 10% with 9.1% average EDP gain, while surpassing a state-of-the-art technique.

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**Sangeet Saha** is currently associated with the Embedded and Intelligent Systems (EIS) Research Group, University of Essex, UK as a Lecturer. Prior to that, he worked as a lecturer at the University of Huddersfield, UK, and Senior research officer (Postdoctoral scholar) at the University of Essex, UK. His current research interests include real-time scheduling, scheduling for reconfigurable computers, real-time and fault-tolerant embedded systems, and cloud computing. He published several of his research contributions in conferences like CODES+ISSS, ISCAS, Euromicro DSD, and in journals like ACM TECS, IEEE TCAD, IEEE TSMC.



**Shounak Chakraborty** (Senior member, IEEE) is currently working as a guest researcher at the Department of Computer Science, NTNU, Norway. Primarily, his research interests include high performance computer architectures, emerging memory technologies, on-chip thermal management, and compilers. Prior to joining NTNU, Shounak obtained his PhD degree in Computer Science and Engineering from IIT Guwahati, India in February 2018, and also worked as assistant professor at IIIT Guwahati, India.



**Sukarn Agarwal** is an Assistant Professor at School of Computing and Electrical Engineering, IIT Mandi (India). He has earned his PhD degree in Computer Science and Engineering from IIT Guwahati, India, in March 2020, and was also a senior research fellow at School of Informatics, University of Edinburgh (UK). His research interests include Emerging Memory Technologies, Memory System Design, Network-on-Chip design and Thermal Aware Chip Management. He published many of his research contributions in conferences like IPDPS, DAC, PLDI, ASAP, VLSI-SoC, GLS-VLSI, etc. and also published several of his research outcomes in journals like IEEE TVLSI, ACM TECS, IEEE TC, IEEE TPDS, and ACM TODAES.



**Magnus Själander** is working as a Professor at the Norwegian University of Science and Technology (NTNU). He obtained his Ph.D. from Chalmers University of Technology in 2008. Before joining NTNU in 2016 he has been a researcher at Chalmers University of Technology, Florida State University, and Uppsala University. Själander's research interests include hardware/software co-design (compiler, architecture, and hardware implementation) for high-efficiency computing.



**Klaus McDonald-Maier** is currently the Head of the Embedded and Intelligent Systems Laboratory and Director Research, University of Essex, Colchester, U.K. He is also the founder of UltraSoC Technologies Ltd., the CEO of Metrarc Ltd., and a Visiting Professor with the University of Kent. His current research interests include embedded systems and system-on-chip design, security, development support and technology, parallel and energy-efficient architectures, computer vision, data analytics, and the application of soft computing and image processing techniques for real-world problems. He is a member of VDE and a Fellow of the BCS and IET.